South East Asian J. of Mathematics and Mathematical Sciences Vol. 15, No. 3 (2019), pp. 81-92

ISSN (Online): 2582-0850

ISSN (Print): 0972-7752

ON CERTAIN CAYLEY-ORR IDENTITIES OF SPECIAL TYPE

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(Received: Jul. 05, 2019 Accepted: Sep. 12, 2019 Published: Dec. 31, 2019)

Abstract: In this paper, making use of certain known transformations of polybasic hypergeometric series we establish some Cayley-Orr type of identities which are of number theoretic importance.

Keywords and Phrases: Cayley- Orr identities, poly- basic, transformations, generalized hypergeometric functions, q-series.

2010 Mathematics Subject Classification: 33A30, 33A15.

1. Notations and Definitions

We shall follow the following notations and definitions in this paper. We define a generalized hypergeometric function, ${}_rF_s$ as,

$$_{r}F_{s}\begin{bmatrix} (a_{r}); z \\ (b_{s}) \end{bmatrix} = \sum_{n=0}^{\infty} \frac{(a_{1})_{n}(a_{2})_{n}...(a_{r})_{n}z^{n}}{(1)_{n}(b_{1})_{n}(b_{2})_{n}...(b_{s})_{n}}$$
 (1.1)

where the symbol

$$(\alpha)_n = \begin{cases} \alpha(\alpha+1)(\alpha+2)...(\alpha+n-1); & n>0\\ 1; & n=0 \end{cases}$$